# ČESKÁ ZEMĚDĚLSKÁ UNIVERZITA V PRAZE <br> PROVOZNĚ EKONOMICKÁ FAKULTA 

CESKA
ZEMÉDELLSKA
UNIVERZITA VPRAZE

## Mathematics - Recommended time of processing : 45 minutes

1) The set of all solutions of the inequality $\frac{3}{1-x}<1$ in the domain R is:
a) $(-\infty,-2)$
b) $(-\infty,-2) \cup(1,+\infty)$
c) $(-2,1)$
d) $(1,+\infty)$
e) none of the answers above is correct
2) The definition domain of the function $y=\frac{\sqrt{1-x}}{\log (x-1)}$ is the set :
a) $\varnothing$
b) $\{1\}$
c) $(-1,1)$
d) $\mathrm{R}-\{1\}$
e) none of the answers above is correct
3) The goniometric form of the complex number $-\frac{1}{2}-\frac{\sqrt{3}}{2} i$ is equal to :
a) $\cos \frac{4}{3} \pi+i \sin \frac{4}{3} \pi$
b) $\cos \frac{5}{3} \pi+i \sin \frac{5}{3} \pi$
c) $\sin \frac{\pi}{6}+i \cos \frac{5}{6} \pi$
d) $\sin \frac{5}{6} \pi+i \cos \frac{5}{6} \pi$
e) none of the answers above is correct
4) For an arithmetic sequence it holds $a_{5}-a_{1}=12$, $a_{3}=7$. The $a_{12}$ member is equal to the number :
a) 34
b) 31
c) 27
d) 19
e) none of the answers above is correct
5) One root of the equation $x^{2}+3 \sqrt{n} x+n+1=0$ is a double real root for :
a) $\mathrm{n}=1$
b) $\mathrm{n}=4$
c) $\mathrm{n}=0$
d) $n=4 / 5$
e) none of the answers above is correct
6) Decide which values $x, y \in R$ give the solution of the given set of equations
$\log _{\frac{1}{3}} x-\log _{\frac{1}{3}} y=0 \wedge y^{2}-2 x-3=0:$
a) $x=y=0$
b) $x=y=3$
c) $x=0, y=3$
d) $x=3, y=0$
e) none of the answers above is correct
7) The function $\mathrm{y}=-5 \cdot \frac{|x|}{x}$ is over the whole definition domain
a) even, increasing
b) even, decreasing
c) odd, increasing
d) odd, decreasing
e) none of the answers above is correct
8) The set of all solutions of the equation $(1-\cos x)(2-\sin x)=0$ is the set :
a) $\left\{(2 \mathrm{k}+1) \frac{\pi}{2}, \mathrm{k} \in \mathrm{Z}\right\}$
b) $\{\mathrm{k} \pi, \mathrm{k} \in \mathrm{Z}\}$
c) $\{2 \mathrm{k} \pi, \mathrm{k} \in \mathrm{Z}\}$
d) $\{(2 \mathrm{k}+1) \pi, \mathrm{k} \in \mathrm{Z}\}$
e) none of the answers above is correct
9) The number of points of the circle $x^{2}+y^{2}-6 x-10 y+9=0$ common with the axes of coordinates is equal to the number :
a) 0
b) 1
c) 2
d) 3
e) none of the answers above is correct
10) The straight lines $p: 3 x+4 y-2=0$ and q: $8 x-6 y+4=0$ are closing an angle of size :
a) $\pi / 6$
b) $\pi / 3$
c) $\pi / 2$
d) $2 \pi / 3$
e) none of the answers above is correct
11) All real solutions of the equation $4^{x+3}-4^{x}=63$ belong to the interval :
a) $\langle-1,0$,
b) $\langle 0,1)$
c) $\langle 1,2)$
d) $\langle 2,4)$
e) none of the answers above is correct
12) Define the number $y \in R$ such, that the point $A=[2, y]$ is situated on the straight line which is paralell with the line $y=4 x+5$ and is passing the point $\mathrm{B}=[1,4]$ :
a) $y=4$
b) $y=8$
c) $y=9$
d) $y=13$
e) none of the answers above is correct
13) The negation of statement „At least one dog does not bite" is the statement :
a) One dog bites.
b) All dogs do not bite.
c) More than one dog bite.
d) All dogs bite.
e) none of the answers above is correct
14) The absolute value of complex number $z=i^{58}+i^{160}$ is equal to the number :
a) 0
b) 2
c) 1
d) i
e) e) none of the answers above is correct
15) The equation $\log _{3} 27 x+\log _{3} x^{2}=15$ has one root only, that is situated within the interval :
a) $(71,83)$
b) $(49,57)$
c) $(27,50)$
d) $(3,15)$
e) none of the answers above is correct
16) The number of all real solutions of the equation $\sqrt{5-x}=x+1$ is equal to the number :
a) 1
b) 2
c) 3
d) 0
e) none of the answers above is correct
17) Establish value of the expression $\frac{3 \sin x+\cos x}{\cos x-3 \sin x}$,
if the $\operatorname{cotg} x=1$ :
a) 0
b) 1
c) 2
d) -2
e) none of the answers above is correct
18) The circle drawn around a rectangular triangle with legs long $\sqrt{2}$ is itself long:
a) $\sqrt{2 \pi}$
b) $6 \pi$
c) $4 \pi$
d) $2 \pi$
e) none of the answers above is correct
19) For every $x \geq 0$ the expression $\sqrt{x \cdot \sqrt[3]{\sqrt{x}}}$ is equal to:
a) $x^{\frac{7}{6}}$
b) $x^{\frac{5}{6}}$
c) $x^{\frac{7}{12}}$
d) $x^{\frac{3}{2}}$
e) none of the answers above is correct
20) The number of common points of the parabola $y^{2}=8 x$ and the straight line $p: x+y=0$ is equal to :
a) 2
b) 1
c) 0
d) $\infty$
e) none of the answers above is correct
