ČESKÁ ZEMĚDĚLSKÁ UNIVERZITA V PRAZE PROVOZNĚ EKONOMICKÁ FAKULTA

Mathematics - Recommended time of processing: 45 minutes

- 1) The set of all solutions of the inequality $\frac{3}{1-x} < 1$
 - in the domain R is:
 - a) $(-\infty, -2)$
 - b) $(-\infty, -2) \cup (1, +\infty)$
 - c) (-2, 1)
 - d) $(1, +\infty)$
 - e) none of the answers above is correct
- 2) The definition domain of the function $y = \frac{\sqrt{1-x}}{\log(x-1)}$
 - is the set:
 - a) Ø
 - b) {1}
 - c) (-1, 1)
 - d) $R \{1\}$
 - e) none of the answers above is correct
- 3) The goniometric form of the complex number
 - $-\frac{1}{2} \frac{\sqrt{3}}{2}i$ is equal to:
 - a) $\cos\frac{4}{3}\pi + i\sin\frac{4}{3}\pi$
 - b) $\cos \frac{5}{3}\pi + i \sin \frac{5}{3}\pi$
 - c) $\sin \frac{\pi}{6} + i \cos \frac{5}{6} \pi$
 - d) $\sin \frac{5}{6}\pi + i \cos \frac{5}{6}\pi$
 - e) none of the answers above is correct
- 4) For an arithmetic sequence it holds $a_5 a_1 = 12$, $a_3 = 7$. The a_{12} member is equal to the number:
 - a) 34
 - b) 31
 - c) 27
 - d) 19
 - e) none of the answers above is correct
- 5) One root of the equation $x^2 + 3\sqrt{n} x + n + 1 = 0$ is a double real root for :
 - a) n = 1
 - b) n = 4
 - c) n = 0
 - d) n = 4/5
 - e) none of the answers above is correct

6) Decide which values $x, y \in R$ give the solution of the given set of equations

the given set of equations
$$\log_{\frac{1}{3}} x - \log_{\frac{1}{3}} y = 0 \wedge y^2 - 2x - 3 = 0$$
:

- a) x = y = 0
- b) x = y = 3
- c) x = 0, y = 3
- d) x = 3, y = 0
- e) none of the answers above is correct
- 7) The function $y = -5 \cdot \frac{|x|}{x}$ is over the whole definit
 - ion domain
 - a) even, increasing
 - b) even, decreasing
 - c) odd, increasing
 - d) odd, decreasing
 - e) none of the answers above is correct
- 8) The set of all solutions of the equation $(1 \cos x) (2 \sin x) = 0$ is the set:
 - a) $\{(2k+1)\frac{\pi}{2}, k \in Z\}$
 - b) $\{k\pi, k \in \mathbb{Z}\}$
 - c) $\{2k\pi, k \in \mathbb{Z}\}$
 - d) $\{(2k+1)\pi, k \in \mathbb{Z} \}$
 - e) none of the answers above is correct
- 9) The number of points of the circle $x^2 + y^2 6x 10y + 9 = 0$ common with the axes of coordinates is equal to the number:
 - a) 0
 - b) 1
 - c) 2
 - d) 3
 - e) none of the answers above is correct
- 10) The straight lines p: 3x + 4y 2 = 0 and
 - q: 8x 6y + 4 = 0 are closing an angle of size :
 - a) $\pi/6$
 - b) $\pi/3$
 - c) $\pi/2$
 - d) $2\pi/3$
 - e) none of the answers above is correct

- 11) All real solutions of the equation $4^{x+3} 4^x = 63$ belong to the interval:
 - a) $\langle -1, 0, \rangle$
 - b) (0, 1)
 - c) (1, 2)
 - d) (2,4)
 - e) none of the answers above is correct
- 12) Define the number $y \in R$ such, that the point A = [2, y] is situated on the straight line which is parallel with the line y = 4x+5 and is passing the point B = [1, 4]:
 - a) y = 4
 - b) y = 8
 - c) y = 9
 - d) y = 13
 - e) none of the answers above is correct
- 13) The negation of statement "At least one dog does not bite" is the statement :
 - a) One dog bites.
 - b) All dogs do not bite.
 - c) More than one dog bite.
 - d) All dogs bite.
 - e) none of the answers above is correct
- 14) The absolute value of complex number $z=i^{58}+i^{160}$ is equal to the number :
 - a) 0
 - b) 2
 - c) 1
 - d) i
 - e) e) none of the answers above is correct
- 15) The equation $log_3 27x + log_3 x^2 = 15$ has one root only, that is situated within the interval :
 - a) (71, 83)
 - b) (49, 57)
 - c) (27, 50)
 - d) (3, 15)
 - e) none of the answers above is correct
- 16) The number of all real solutions of the equation $\sqrt{5-x} = x+1$ is equal to the number :
 - a) 1
 - b) 2
 - c) 3
 - d) 0
 - e) none of the answers above is correct

17) Establish value of the expression $\frac{3\sin x + \cos x}{\cos x - 3\sin x}$,

if the $\cot x = 1$:

- a) 0
- b) 1
- c) 2
- d) -2
- e) none of the answers above is correct
- 18) The circle drawn around a rectangular triangle with legs long $\sqrt{2}$ is itself long:
 - a) $\sqrt{2\pi}$
 - b) 6π
 - c) 4π
 - d) 2π
 - e) none of the answers above is correct
- 19) For every $x \ge 0$ the expression $\sqrt{x} \cdot \sqrt[3]{\sqrt{x}}$ is equal to:
 - a) $x^{\frac{7}{6}}$
 - b) $x^{\frac{5}{6}}$
 - $\frac{1}{2}$
 - c) x^{12}
 - d) $x^{\frac{3}{2}}$
 - e) none of the answers above is correct
- 20) The number of common points of the parabola $y^2 = 8x$ and the straight line p: x+y=0 is equal to:
 - a) 2
 - b) 1
 - c) 0
 - d) ∞
 - e) none of the answers above is correct